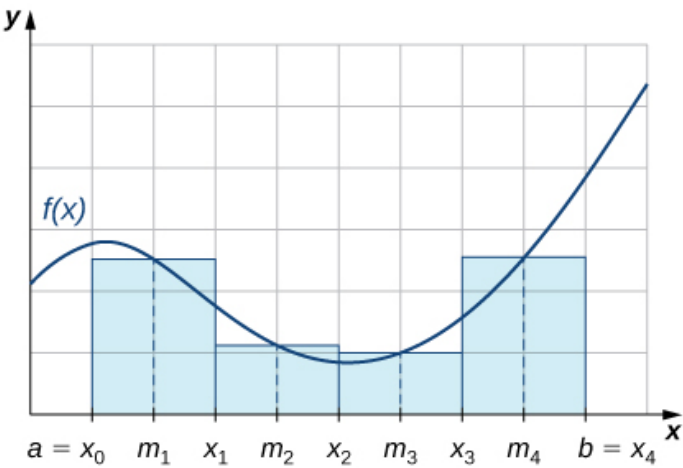


# MATH 130A Review: Midpoint Rule

## Facts to Know

Integration approximation with the midpoint rule

Picture example



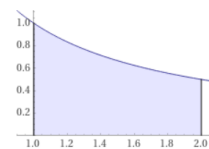
Formal definition

$$\int_a^b f(x) dx \approx \sum_{i=1}^n f(m_i) \Delta x,$$

where

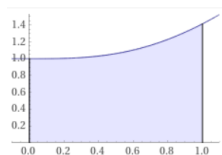
## Examples

- Use the midpoint rule with  $n = 5$  to approximate  $\int_1^2 \frac{1}{x} dx$



$\approx \underline{0.69315}$

- Use the midpoint rule with  $n = 5$  to approximate  $\int_0^1 \sqrt{x^3 + 1} dx$



$\approx \underline{1.11145}$

- Use the midpoint rule with  $n = 4$  to approximate  $\int_0^8 \sin \sqrt{x} dx$



$\approx \underline{5.9979}$